

Name:

Date:

Period:

### Writing the Equation of a Line

There are two different formats for writing the equation of a line.

## Slope – intercept Form

$$y = mx + b$$

↑ slope      ↑ y-intercept

Slope-intercept form is useful when we know the y - intercept of a line.  
 However, we are not always given this information.

## Point - Slope Form

$$(y - y_1) = m(x - x_1)$$

↙ y - value from point given      ↑ slope      ↖ x - value from point given

When we know the slope and one point (**not** the y-intercept), we can write the equation in point - slope form.

### 1. When given the slope and y-intercept: Use Slope-Intercept Form

- 1] Substitute for m
- 2] Substitute for b
- 3] Write your equation in  $y = mx + b$  format

**For example:** Write the equation of the line whose slope is -3 and y-intercept is 8.

$$y = -3x + 8$$

**YOUR TURN:** Write the equation of the line whose slope is 4 and y-intercept is -2.

### 2. When given the slope and one point: Use either format

**For example:** Write the equation (using EACH format) of the line whose **slope is 4** that passes through the point **(3, 5)**.

#### Using Slope-Intercept Form

- 1] Substitute for m
- 2] Substitute for x and y from the point (x, y)
- 3] Solve for b
- 4] Write the equation in  $y = mx + b$  format.

#### Using Point – Slope Form

- 1] Substitute for m
- 2] Substitute for  $x_1$  and  $y_1$  from the point (x, y)
- 3] Verify

1] Substitute for m:

$$y = mx + b$$

$$y = 4x + b$$

2] Substitute for x and y:

$$y = 4x + b$$

$$5 = 4(3) + b$$

1] Substitute for m:

$$(y - y_1) = m(x - x_1)$$

$$(y - y_1) = 4(x - x_1)$$

2] Substitute for  $x_1$  and  $y_1$ :

$$(y - 5) = 4(x - 3)$$

This is the format you should leave your equation in

3] **Solve** for b:

$$5 = 12 + b$$

$$-12 = -12$$

$$-7 = b$$

4] Write in  $y = mx + b$  format

$$y = 4x - 7$$

To verify this equation, if you distribute and solve for y, you should get the same  $y = mx + b$  equation:

$$y - 5 = 4x - 12$$

$$\begin{array}{r} + 5 \quad + 5 \\ \hline y = 4x - 7 \end{array}$$

These should match

**YOUR TURN:** Write the equation (using EACH format) of the line whose slope is 2 that passes through the point (-3, 4).

Using Slope-Intercept Form:

Using Point – Slope Form

1] Substitute for m:	2] Substitute for x and y:	1] Substitute for m:	2] Substitute for $x_1$ and $y_1$ :
3] <b>Solve</b> for b:	4] Write in $y = mx + b$ format	Verify:	

**3. When given two points: Use either format**

**For example:** Write the equation (using EACH format) of the line that passes through the points (2, 5) and (4, 11).

Using Slope-Intercept Form:

Using Point – Slope Form

1] Find m using the slope formula	1] Find m using the slope formula
2] Substitute for m	2] Substitute for m
3] Substitute for x and y from EITHER point (x, y)	3] Substitute for $x_1$ and $y_1$ from EITHER point (x, y)
4] Solve for b	4] Verify
5] Write the equation in $y = mx + b$ format.	

1] Find m (since the first step is the same for both formats, you only have to find the slope once:

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{11 - 5}{4 - 2} = \frac{6}{2} = 3$$

2] Substitute for m: $y = \underline{m}x + b$ $y = \underline{3}x + b$	3] Substitute for x and y: $y = \underline{3x} + b$ $\underline{5} = 3(\underline{2}) + b$	2] Substitute for m: $(y - y_1) = \underline{m}(x - x_1)$ $(y - y_1) = \underline{3}(x - x_1)$	3] Substitute for $x_1$ and $y_1$ : $(y - 5) = \underline{3}(x - 2)$ This is the format you should leave your equation in
4] <b>Solve</b> for b: $5 = 3(2) + b$ $5 = 6 + b$ $\underline{-6} = \underline{-6}$ $-1 = b$	5] Write in $y = mx + b$ format $y = 3x - 1$	Verify:	

**YOUR TURN:** Write the equation (using EACH format) of the line that passes through the points (3, 1) and (9, 7).

1] Find m:

2] Substitute for m:	3] Substitute for x and y:	2] Substitute for m:	3] Substitute for $x_1$ and $y_1$ :
4] <b>Solve</b> for b:	5] Write in $y = mx + b$ format	Verify:	