

Name:

Date:

Period:

Explicit Formula
Used to find specific "place in line"

Arithmetic	Geometric
$a_n = a_1 + d(n - 1)$	$a_n = (a_1)(r)^{n-1}$
a_1 is the initial value d is the common difference (the amount added to advance from one term to the next)	a_1 is the initial value r is the common ratio (the amount by which each term is multiplied to advance to the next term)

Example:

Write the explicit formula for the following sequence:
9, 16, 23, 30

Example:

Write the explicit formula for the following sequence:
-1, 3, -9, 27

Initial Value	Common Difference	Equation*	Initial Value	Common Ratio	Equation
9	⇒ +7 ⇒	$a_n = 9 + 7(n - 1)$	-1	⇒ -3 ⇒	$a_n = (-1)(-3)^{n-1}$

*Simplify the equation into $y = mx + b$ format:

$$a_n = 9 + 7n - 7 \quad \Rightarrow \quad a_n = 7n + 2$$

Practice Problems:

1. Write the equation for the arithmetic sequence using sequence notation.

11, 16, 21, 26, 31, ...

2. Write the equation for the geometric sequence using sequence notation.

5, 15, 45, 135, 405, ...

Initial Value	Common Difference	Equation*	Initial Value	Common Ratio	Equation

Simplify: _____ ⇒ _____

3. Write the equation for the arithmetic sequence using sequence notation.

-29, -34, -39, -44, -49

4. Write the equation for the geometric sequence using sequence notation.

-4, 8, -16, 32, -64

Initial Value	Common Difference	Equation*	Initial Value	Common Ratio	Equation

Simplify: _____ ⇒ _____

5. Write the equation for the arithmetic sequence using sequence notation.

-34, -26, -18, -10, -2

6. Write the equation for the geometric sequence using sequence notation.

5, 25, 125, 625, ...

Initial Value	Common Difference	Equation*	Initial Value	Common Ratio	Equation

Simplify: _____ ⇒ _____

A sequence can also be described with a **recursive formula** that gives the initial term and the relationship between consecutive terms.

Recursive Formula Uses previous term to find next term

Arithmetic	Geometric
$a_1 = \text{first term}$ $a_n = a_{n-1} + d$	$a_1 = \text{first term}$ $a_n = (a_{n-1})(r)$
a_1 must be given $a_{n-1} = \text{previous term}$	r is the common ratio (the amount by which each term is multiplied to advance to the next term)
d is the common difference (the amount added to advance from one term to the next)	

<p>Example: Write the recursive formula for the following sequence: 9, 16, 23, 30</p>	<p>Example: Write the recursive formula for the following sequence: -1, 3, -9, 27</p>
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Initial Value	Common Difference	Equation*	Initial Value	Common Ratio	Equation*
9	+7	$a_1 = 9$ $a_n = a_{n-1} + 7$	-1	-3	$a_1 = -1$ $a_n = (a_{n-1})(-3)$

* When writing the equation for a recursive formula, you **MUST** include a_1 as part of the equation

Practice Problems:

<p>1. Write the recursive formula for the following sequence: -17, -11, -5, 1</p>	<p>2. Write the recursive formula for the following sequence: -4, 12, -36, 108</p>												
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<p>3. Write the recursive formula for the following sequence: -1, 9, 19, 29</p>	<p>4. Write the recursive formula for the following sequence: 4, -20, 100, -500</p>												
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<p>5. Write the recursive formula for the following sequence: 9, 11, 13, 15</p>	<p>6. Write the recursive formula for the following sequence: 3, 6, 12, 24, 48</p>												
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